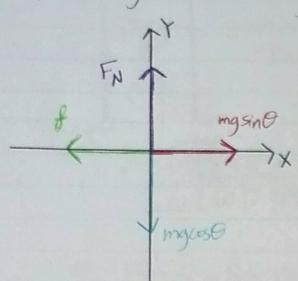
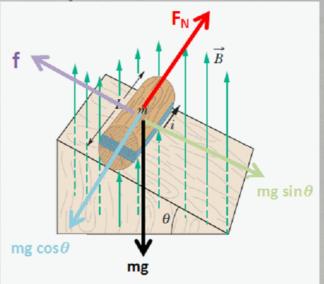
[28-7] The below Figure shows a wood cylinder of mass m= 0.150 kg and Length L = 0.100 m, with N = 13.0 turns of wire wrapped around it longitudinally, so that the plane of the wire coil contains the long central axis of the cylinder, The cylinder is released on a plane inclined at an angle O to the horizontal, with the plane of the coil parallel to the incline plane. If there is a vertical uniform magnetic field of magnitude 0.92 T, What is the Least current & through the coil that keeps the cylinder from rolling down the plane?





· Newton's Second Law for the COM of cylinder mg sino -f = ma

. Newton'r Second Law for rotation about the center of the cylinder  $T = I \times$ 

The magnetic held produces a torque on the current-Carrying coil T = MXB, T = MB sin O "Counterdock wise angular acceleration

> Friction force produces a torque (T=fr), r = cylinder radius.

> I = IX > fr - MB sin0 = IX

· Keeps the cylinder from rolling down the plane  $\alpha = x = 0$ Translational and Rotational Equilibrium

The Loop is rectangular, A = 2rL and the magnitude of magnetic dipole moment U = NiA = Ni2rL mqr = 2NirLB

$$\hat{l} = \frac{0.150 \times 9.8}{2 \times 13 \times 0.1 \times 0.92} = 0.61 \text{ A}$$

Note The Friction force tries to make the cylinder to roll down while the current creates a torque that tries to make it go uphill

28-8 In the below Figure, A charged particle moves into a region of uniform magnetic field B, goes through half a circle, and then exists that region. The particle is either a proton or an electron (You must decide which). It spends 160 ns in the region. (a) What is the magnitude of BP (b) If the particle is sent back through the magnetic field (along the same initial path) but with 2.00 times its previous kinetic energy, how much time does it spend in the field during this trip?

- At point A, which it enters the held-hilled region.

a) 
$$T = \frac{2Tm}{191B}$$

proton 
$$\Rightarrow T = \frac{2\pi m_p}{eB}$$
,  $2 \times 160 \times 10^{-9} = 2\pi (1.67 \times 10^{-27})$ 

b) The period time T does not depend on speed [T = 2Tm/1918],

But doupling the kinetic energy will increase the speed by N'=12N

$$KE' = 2KE \Rightarrow \pm mv^2 = 2(\pm mv^2) \Rightarrow v' = \sqrt{2}v$$

So the radius of the path will be r'= 12 r

28-10 The bent wire shown in the below Figure Lies in a uniform magnetic field. Each straight section is 2.0m Long and makes an angle of  $\theta = 60^{\circ}$  with the X-axis, and the wire carries a current of 3.5A. What is the net magnetic force on the wire in unit vector notation if the magnetic field is given by a) 4.0k T and b) 4.0î T?

. Magnetic Force on a current carrying wire

$$\overrightarrow{F_B} = 2 \overrightarrow{L} \times \overrightarrow{B}$$

$$\rightarrow \overrightarrow{L}_1 = L(\cos\theta \hat{c} + \sin\theta \hat{j})$$

· Bent-wire

Wire, of dimensions 10:0 cm by 5:0 cm. It carries a current of 0.80A and is hinged along one long side. It is mounted in the xy plane, at angle 0 = 25° to the direction of a uniform magnetic hield of magnitude 0.50 T. In unit-vector rotation, what is the torque acting on the coil about the hing line?

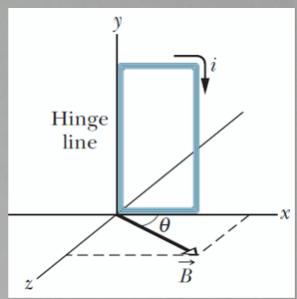
Torque on a current-carraying loop

•  $\vec{\mu}$  = magnetic dipole moment  $M = N^{\circ}A$  in negative Z-direction  $\vec{\mu} = 28 \times 0.8 \times 5 \times 10 \times 10^{-4} (-\hat{k})$   $\vec{\mu} = (0.112 \text{ A.m}^{2})\hat{k}$   $\Rightarrow \text{ Let } \vec{B} = \text{B casO}2 + \text{B sinO}\hat{k}$ 

M=-MR

$$\vec{T} = -0.112 \times 0.5 \cos(25)$$

$$= -(0.0508 \, \text{N.m.})$$



128-22 A metal strip 6.50 cm long, 0.850 cm wide, and 0.760mm thick moves with constant velocity v through a uniform magnetic held B = 1.20mT directed perpendicular to the strip, as shown in the below figure, Apotential difference of 3.30MV is measured between points X and y across the strip. Calculate the speed v?

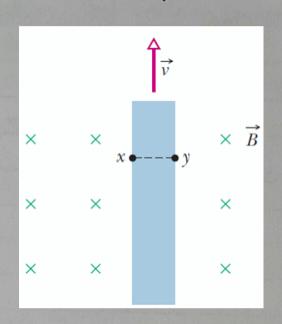
The force on a free charge of inside the metal strip with velocity in F = q[E+ixB]

By Newton's Second Low F=ma

 $\Rightarrow$  mover with constant velocity  $\vec{a} = 0 \Rightarrow \vec{F_B} = \vec{F_E}$ 

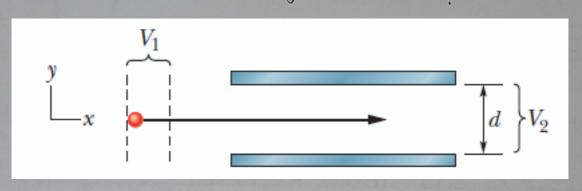
$$v = \frac{E}{B}$$
,  $E = \frac{V_x - V_y}{dxy}$ 

$$v = \frac{3.3 \times 10^{-6}}{0.85 \times 10^{-2} \times 1.2 \times 10^{-3}} = 0.324 \text{ m/s}$$



28-31 In the below figure, an electron accelerated from rest through potential difference  $V_1 = 2.50 \, \text{KV}$  enters the gasp between two parallel plates having separation  $d = 16.0 \, \text{mm}$  and potential difference  $V_2 = 100 \, \text{V}$ . The lower plate is at the lower potential. Neglect fringing and assume that the electron's velocity vector is perpendicular to the electric field vector between the plates. a) In unit-vector notation, what uniform magnetic field allows the electron to travel in a straight line in the gap?

b) If the potential difference is increased slightly, in what direction does the electron veer from straight line motion?



a) Electron travels in astraight line in the gap 
$$\Rightarrow$$
  $\vec{F}_{net} = 0$ 

$$\vec{F} = q(\vec{E} + \vec{V} \times \vec{B}) = 0 \quad |\vec{V} \perp \vec{B} \text{ given } |$$

$$E = VB \quad \Rightarrow \text{ By using conservation } f \text{ a mechanical energy}$$

$$qV = \frac{1}{2} m V^2 \quad \text{Electric potential} \rightarrow \text{ Kinetic energy}$$

$$V = \sqrt{\frac{2eV}{me}}$$

$$B = \frac{E}{V} = \frac{100/(16\times10^{-3})}{\sqrt{2\times1.6\times10^{-19}\times2.5\times10^{3}/9.11\times10^{-31}}} = 0.211\times10^{3} \text{ T}$$

⇒ Lower plate is at the Lower potential

Electric Force on electron upward

magnetic Force on electron Journward

B into the page

B = -(0.211mT) k

FB PELONIN

b) Potential difference increases > velocity increases > Electric hield increases > Electric Force increases > Electron weer towards upper plate.

28-37 An electron moves through a uniform magnetic field given by  $\vec{B} = B_X t + (-3.0 B_X) j$ . At a particular instant, the electron has velocity  $\vec{v} = (2.0 \hat{i} + 4.0 \hat{j})$  m/s and the magnetic force acting on it is  $(6.4 \times 10^{-19} \, \text{N}) \hat{k}$ . Find  $B_X$ ?

$$(6.4 \times 10^{19} \,\text{N})\hat{k} = -e(2.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

$$= -e(2.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

$$= -e(2.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

$$= -e(2.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

$$= -e(3.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

$$= -e(3.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

$$= -e(3.0\hat{c} + 4.0\hat{j}) \times (B_{x}\hat{c} + (-3.0 \,\text{B}_{x})\hat{j})$$

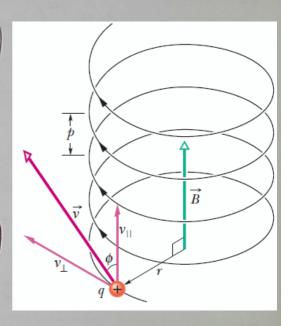
$$B_{X} = \frac{6.4 \times 10^{-19}}{1.6 \times 10^{-19} \times 10} = 0.4 T$$

[28-41] An electron follows a helical path in a uniform magnetic field of magnitude 1.30T. The pitch of the path is 6.00 Mm, and the magnitude of the magnetic force on the electron is 200×10 MM. What is the electron speed?

. Magnetic Force on the electron  $\Rightarrow \vec{F}_B = -e \vec{\nabla} \times \vec{B}$   $\vec{F}_B = e \vec{\nabla}_{\perp} \vec{B}$ 

$$\Rightarrow N_{II} = \frac{PeB}{2\pi me} = \frac{6.0 \times 10^{-6} \times 1.6 \times 10^{-19} \times 1.3}{2\pi (9.11 \times 10^{-31})}$$

$$\Rightarrow V_{\perp} = \frac{F_{B}}{eB} = \frac{2 \times 10^{-14}}{1.6 \times 10^{-19} \times 1.3}$$



. The electron speed

$$=\sqrt{(2.18\times10^5)^2+(0.96\times10^5)^2}=2.38\times10^5 \text{ m/s}$$

[28-63] An electron that has an instantaneous velocity of  $\vec{a} = (-5.0 \times 10^6 \text{ m/s})\hat{i} + (3.0 \times 10^6 \text{ m/s})\hat{j}$  is moving through the uniform magnetic held  $\vec{B} = (0.030 \text{ T})\hat{i} - (0.15 \text{ T})\hat{j}$ . a) Find the Force on the electron due to the magnetic held. b) Repeat your calculation for a proton having the same velocity?

a) 
$$\vec{F}_B$$
 on the electron =  $-e \vec{\Sigma} \times \vec{B}$   
=  $-e \mid \hat{C} \quad \hat{J} \quad \hat{k} \mid$   
 $|-5 \times 10^6 \quad 3 \times 10^6 \quad 0 \mid$   
 $|0.03 \quad -0.15 \quad 0 \mid$